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Stochastik 2 - Presence-Exercises 10:

Presence-Exercise 10.I:

Remember **Presence-Exercise 9.1** where we computed $p_{11}(t)$ of the *Q*-matrix

$$Q = \begin{pmatrix} -2 & 1 & 1\\ 1 & -1 & 0\\ 2 & 1 & -3 \end{pmatrix}.$$

Compute an invariant distribution of Q and compare it with $\lim_{t \nearrow \infty} p_{1,1}(t)$.

Presence-Exercise 10.II:

Consider a fleet of N = 3 buses. Each bus breaks down independently at rate μ , when it is sent to the depot for repair. The repair shop can only repair one bus at a time and each bus takes an exponential time of parameter λ to repair. Find the invariant distribution of the number of buses in service.

Presence-Exercise 10.III:

Consider the above Presence-Exercise 10.II, but...

- 1. ... consider that the repair shop can repair 2 buses at once.
- 2. ... consider that the repair shop can repair 3 buses at once.